Modeling of Soot Formation in Internal Combustion Engines

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Introduction

Soot formation is a complex process, which incorporates many chemical and physical steps: (1) homogeneous inception of large molecular precursors, (2) surface growth in the reactions with the gas-phase active species, (3) coalescent coagulation to form larger particles, and, finally, (4) agglomeration of the primary particles to form chain-like aggregates.

The formation of molecular precursors is the first important step in the course of soot formation. Regardless the initial fuel involved, the hydrocarbon fuel undergoes either pure or oxidative pyrolysis, degrading into small hydrocarbon radicals. Under fuel-rich conditions, the small radicals react, leading to the formation of smaller hydrocarbons, particularly acetylene ($C_2H_2$). Then, large hydrocarbon molecules containing a sufficiently large number of carbon atoms such as polyynes ($C_{2n}H_2, n = 2, 3, ...$) and polycyclic aromatic hydrocarbons (PAHs) are built up, that are commonly regarded as the molecular soot precursors.

Depending on the type of molecular precursors assumed to be present, several competing theories, such as the PAH model or the polyyne model, have been proposed. In the H-abstraction-acetylene-addition (HACA) mechanism, aromatic species like benzene, toluene, naphthalene, etc. are considered as islands of stability in an infinite sea of possible molecular structures which might be formed through molecular growth. The polyyne model assumes that every radical capable of forming polyyne complexes becomes a center of polymerization. A polyyne molecule and a polyyne radical or two polyyne molecules react to form the polyyne complexes. Under high temperature conditions, when C-H bonds are relatively loose, the carbon skeletons of acetylene and polyyne molecules persist in the gas-phase as the most stable structures of small carbon clusters due to their high thermodynamic stability. Recent experiments and theoretical studies [1, 2] have discovered that the most stable structures of carbon clusters up to $C_{20}$ are chains and monocycles. This finding supports the polyyne mechanism recently developed on the basis of the fast chemical aggregation theory in the works [3-5].

For modeling soot formation in internal combustion engines using CFD software there is a need in simple and efficient soot models predicting satisfactorily the soot yield under different operation conditions. The detailed
kinetic models of soot formation incorporating all the processes mentioned above can be used for validating such models.

The objective of this study was to develop a computationally efficient overall soot model based on the detailed soot formation model.

1 Detailed mechanism

Semenov Institute of Chemical Physics has been involved in soot formation modeling for a long time. Recently, the most detailed mechanism of soot formation has been developed by joint efforts of Semenov Institute and Universität Heidelberg. For example, Vlasov and Warnatz [6] reported the kinetic scheme of soot formation process during pyrolysis of various aliphatic and aromatic hydrocarbons. It combines the mechanisms of formation of polyaromatic hydrocarbons, polyynes, two mechanisms of soot precursor formation due to condensation of polyaromatic and polyyne molecules, soot particle growth by the reactions of HACA mechanism and polyyne molecule addition, the mechanism of acetylene pyrolysis and pure carbon cluster formation. Later, the mechanism of \( n \)-heptane oxidation was added into this detailed kinetic scheme of soot formation process. As a result, the complete detailed kinetic scheme of soot formation process incorporates 1850 gas-phase reactions between 186 species and 100 heterogeneous reactions with participation of four ensembles of microheterogeneous particles of different types. The rate coefficients of some important reactions have pressure dependence. Thus, the gas phase reaction mechanism consists of a complete kinetic scheme of polyaromatic hydrocarbon formation developed in [7] for laminar premixed acetylene and ethylene flames with all corrections presented in [8], the kinetic scheme of acetylene pyrolysis proposed in [9] and [10], the kinetic scheme of polyyne molecule formation developed in [3, 4], the kinetic scheme of pure carbon cluster formation up to \( C_{30} \) presented in [11-13], and the kinetic scheme of \( n \)-heptane oxidation developed in [14].

The gas-phase kinetic scheme of polyaromatic hydrocarbon formation describes the pyrolysis and oxidation of \( C_1 \) and \( C_2 \) species, the formation of higher linear hydrocarbons up to \( C_6 \) species, the formation of benzene and further reactions leading to pyrene and the oxidation pathways of the aromatic species. The gas-phase reaction mechanism of the model considered consists of the reactions of the following species: \( \text{H}_2/\text{O}_2 \), \( \text{HO}_2/\text{H}_2\text{O}_2 \), \( \text{CO/CO}_2 \), \( \text{C/CO}/ \ldots /\text{C}_{30} \), \( \text{CH,HCO,CH}_2 \), \( \text{CH}_2^* \), \( \text{CH}_3 \), \( \text{CH}_3\text{O}/\text{CH}_2\text{OH,CH}_4,\text{CH}_3\text{OH, C}_2\text{H, HCCO, C}_2\text{H}_2,\text{CH}_2\text{CO/HCCOH,C}_2\text{H}_3,C_2\text{H}_4,C_2\text{H}_5, C_2\text{H}_6, C_2\text{O,C}_2\text{H}_3\text{O, C}_2\text{H}_2/C_2\text{H}_3/C_2\text{H}_4, C_4\text{H}/C_4\text{H}_2, C_4\text{H}_3/C_4\text{H}_4, C_4\text{H}_5/C_4\text{H}_6, C_6\text{H}_2/C_6\text{H}_3, C_6\text{H}_4/C_6\text{H}_5, C_6\text{H}_6/C_6\text{H}_7, C_6\text{H}_7/C_6\text{H}_8, \text{benzene/phenyl, polynyes (C}_8\text{H}_2/C_8\text{H}, C_{10}\text{H}_2/C_{10}\text{H}, C_{12}\text{H}_2/C_{12}\text{H}, C_{14}\text{H}_2), \text{phenylacetylene, phenylviny1/styrene, naphthalene, ethynylphenanthrene, phenanthrene, pyrene, biphenyl, benzene oxidation, PAH oxidation by OH, and PAH oxidation by O.} \)
A key aspect of the soot formation process is the deposition of soot mass through reactions of gaseous species with the soot particle surface. In the model available, a minimal mechanism of surface growth of soot particles, presented in [8] is considered. Soot precursors are formed in condensation reactions of pyrene, phenanthrene, and biphenyl molecules (the HACA pathway) and the polyyne molecules C₈H₂, C₁₀H₂, and C₁₂H₂ (the polyyne pathway). The reactions of the soot particles with active sites formed through the HACA pathway with polyyne molecules and polyyne radicals, which create new active sites on their surface, lead to the formation of active soot particles similar to those formed through the polyyne pathway. After this transformation, only active soot particles are considered in the model. These soot particles react with the most reactive gas-phase species (C₂H₂, C₂H, C₂, C₄H₄, C₄H₂, C₄H, C₆H₂, C₆H, C₆, C₈H₂, C₈H, C₈, C₁₀H₂, C₁₀H, C₁₀, C₁₂H₂, C₁₂H, and C₁₂) and participate in condensation reactions with pyrene, phenanthrene, and naphthalene and in coagulation reactions. The soot formation mechanism is included into the MACRON code, which is used for mechanism validation and calculations presented in this report.

For validating the detailed mechanism of soot formation, we compared the results of calculations of the temperature dependencies of the soot yield, the observable rate of soot particle growth and the induction time of soot formation process during pyrolysis of various hydrocarbons for different concentrations of carbon atoms in the reaction mixture with the experimental results obtained by [15] from the cw-laser extinction measurements behind reflected shock waves (Fig. 1). The experimentally measured and calculated values of the soot yield and the induction time of soot formation are in good agreement. This is indicative of a qualitative and quantitative relevance of the kinetic scheme considered.

Next, we compared the experimentally measured [16] and calculated characteristics of soot formation process during rich oxidation of the mixtures of n-heptane, methane, and propane with oxygen under conditions realized behind reflected shock waves at elevated pressures (see Fig. 2). In [16], a combination of the extinction-scattering technique at λ = 488 and 632.8 nm was used for time resolved measurements of soot particle diameter and number density and the traditional extinction technique was applied to determine the soot yield and induction times.

The difference in the soot yield during rich oxidation of various hydrocarbons is not significant. One can suppose that the major portion of a fuel is pyrolyzed with the formation of intermediate species. As they are formed, a competition occurs between molecular growth and oxidative reactions. Whereas the major portion of pyrolysis intermediates is eventually oxidized, a large portion of the carbon-containing species participates in the molecular growth process.
Fig. 1: Temperature dependence of the soot yield in the pyrolysis of benzene/argon mixtures at a pressure of 5.0 MPa for four different concentrations of carbon atoms in the mixture (mol/m³): • [C]=4.0, ■ [C]=1.0, ▲ [C]=0.8, and ● [C]=0.4 mol/m³. Open symbols designate the results of detailed calculations and closed symbols stand for the experimental results. Number density and the traditional extinction technique was applied to determine the soot yield and induction times.

Fig. 2: Experimentally measured (closed symbols) and calculated (open symbols) temperature dependences of the soot yield obtained from the light extinction measurements ($\lambda = 488$ nm) and from the detailed kinetic modeling of soot formation at the reaction time of 3.0 ms for rich oxidation of (circles) $n$-heptane ([C] = 5.9 mol/m³, $\phi = 5$), (squares) methane ([C] = 7.6 mol/m³, $\phi = 5$), and (diamonds) propane ([C] = 6.0 mol/m³, $\phi = 5$), behind shock wave at pressure of 40 bar.

Oxidative reactions lead to a variety of oxygen-containing intermediates and products including CO, CO₂, and H₂O. As a result, the soot yield decreases as compared with the situation of a pure pyrolysis.

The temperature dependences of the mean diameter of soot particles formed during rich oxidation of $n$-heptane obtained from the light scattering measurements ($\lambda = 488$ nm) and calculated with the use of the detailed kinetic model of soot formation were compared for various pressures behind reflected shock wave and a satisfactory agreement was noticed.

The influence of the concentration of carbon atoms in the reacting mixture and the pressure influence behind reflected shock wave on the soot yield during rich oxidation of $n$-heptane were also studied. If the concentration of carbon atoms in the reacting mixture is preserved constant for various pressures, the pressure influence on the soot yield is insignificant and the variation of the concentration of carbon atoms in the reacting mixture, which occurs if the pressure is changed, provides the major contribution into the variation of the soot yield value.

2 Overall Mechanism

The model described in Section 2 cannot currently be implemented into the CFD code due to the excessively large number of reactive species involved and
hence unaffordable CPU time. To overcome this problem we have developed an
approach based on the implications obtained from the analysis of the detailed
mechanism. These implications are listed below:

1. In order to avoid soot yields exceeding 1.0 it is necessary to take into
account fuel depletion in the soot formation reaction.
2. In order to correctly simulate soot oxidation in fuel-rich mixtures, it is
necessary to take into account soot oxidation by both oxygen and water.
3. The reaction steps dealing with hydrogen and carbon monoxide formation
and oxidation in the course of fuel oxidation can be assumed infinitely fast.
Therefore fuel can be assumed to oxidize to CO₂ and H₂O rather than to
CO and H₂O.
4. It can be roughly assumed that oxygen and water are not consumed in the
soot oxidation reactions as it is done in the majority of available overall
soot oxidation mechanisms.

In view of the implications (1) to (4), the new overall mechanism of soot
formation can be represented as follows:

The Symbolic reaction of fuel oxidation is:

\[
1 \text{ kg } C_{cn} H_{hm} + y \text{ kg } (f_{o2} * O_2 + (1.0 - f_{o2}) * N_2) \rightarrow \nonumber \rightarrow \nonumber \rightarrow
(1 + y) \text{ kg } (f_{co} * CO + f_{co2} * CO_2 + f_{h2o} * H_2O + (1.0 - f_{co} - f_{co2} - f_{h2o}) * N_2)
\]

where

\[
hm = 2(cn) + 2\text{ for saturated hydrocarbons, and } f_{o2}, f_{co}, f_{co2}, f_{h2o}\text{ are the}
\]

stoichiometric coefficients of O₂, CO, CO₂ and water, respectively. In terms of
particular species, the symbolic reactions of soot formation and oxidation in
Table 2 are:

**Reaction of soot formation**

\[
C_{cn} H_{hm} + C_{cn} H_{hm}=2(cn)C+Product
\]  (I)

**Reaction of soot oxidation by oxygen**

\[
C+C+O_2=Product
\]  (II)

**Reaction of soot oxidation by water**

\[
C+H_2O=Product
\]  (III)

where “Soot” is represented by the C atom. Since water participates in the soot
oxidation reaction, the “Product” is worth to be attributed to either CO₂ or N₂ in
order to keep minimal the number of reactive species. Each reaction is
characterized by the reaction rate \( W_i \) (\( i = I, II, III \))

\[
W_i = A_i \exp \left( - \frac{E_i}{RT} \right) \prod \left[X_i\right]
\]

where \( T \) is the temperature, \( E_i \) is the activation energy, and \( \prod \left[X_i\right] \) are the products
of volume fractions of species participating in the reaction. The rates of reactions
(I), (II), and (II) are written in the form:
Table 1: Kinetic parameters ($A$ and $E$) of reactions (I), (II) and (III) depending on the mixture equivalence ratio (at pressure ranging from 50 to 200 bar and temperature ranging from 1400 to 3000 K).

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<th>1.54</th>
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<th>4</th>
<th>5</th>
<th>6</th>
<th>8</th>
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<td></td>
<td></td>
<td>E</td>
<td>6.00E+04</td>
<td>6.00E+04</td>
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<td></td>
<td></td>
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<tr>
<td></td>
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</table>

Fig. 3: Soot yield vs. temperature at methane oxidation in air at $p = 50$ atm, and $\Phi = 4$ predicted by the new model (triangles) and detailed (circles) model.

Fig. 4: Soot yield vs. temperature at methane oxidation in air at $p = 50$ atm, and $\Phi = 8$ predicted by the new model (triangles) and detailed (circles) model.

$$W_1 = 2(cn)K_1[X_{C_{cn}H_{hm}}][X_{C_{cn}H_{hm}}]$$
$$W_1 = 2K_1[X_C][X_C][X_O_2]$$
$$W_3 = K_3[X_C][X_{H_2O}]$$

where $K_i = A_i \exp(-E_i/RT)$. Table 1 shows the optimized values of kinetic parameters $A$ and $E$ for reactions (I), (II), and (III). These parameters were
obtained for different values of the equivalence ratio \( \Phi \) (from 1.5 to 8) and for different fuels (methane, propane, and n-heptane). These values are valid for pressures from 50 to 200 bar and temperatures from 1400 to 3600 K. Figures 3 to 6 show

**Fig. 5:** Soot yield vs. temperature at propane oxidation in air at \( p = 50 \) atm, and \( \Phi = 3 \) predicted by the new model (triangles) and detailed (circles) model

**Fig. 6:** Soot yield vs. temperature at n-heptane oxidation in air at \( p = 50 \) atm and \( \Phi = 3 \) predicted by the new model (triangles) and detailed (circles) model

<p>| | |</p>
<table>
<thead>
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<tr>
<td><strong>Table 2:</strong> Engine and injection system data</td>
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<td>Bore</td>
<td>85 mm</td>
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<tr>
<td>Stroke</td>
<td>94 mm</td>
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<tr>
<td>Displacement</td>
<td>533.4 cm³</td>
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<tr>
<td>Compression ratio</td>
<td>16:1</td>
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<tr>
<td>Injection system</td>
<td>BOSCH Piezo CR</td>
</tr>
<tr>
<td>Number of injection holes</td>
<td>8</td>
</tr>
<tr>
<td>Spray angle</td>
<td>158 deg</td>
</tr>
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</table>

the comparison of soot yields predicted by the detailed solution (solid curves) and the new model (dashed curves) at isothermal soot formation with the residence time of 3 ms. It is seen that the new model predicts the bell-shaped curves for the soot yield vs. temperature and provides satisfactory agreement with the detailed model in the most cases considered.

3. Validation of overall model

3.1 Engine and operating conditions

The engine used for the validation study is a single-cylinder research engine with electro hydraulic valve actuation and three intake ports with swirl flaps. An
ω-shaped piston bowl has been chosen for this study (Fig. 7). The main engine and injection system data are summarized in Table 2.

Validation of the overall model is presented for one operating point with conventional Diesel combustion. For this operating point DoE plans have been used for the design of the calculation campaign. This means that for this point a significant number of combustion system variations have been applied by simultaneously changing the start of injection (SOI), residual gas amount (EGR), swirl level and injection pressure. The following table shows the main specifications and the range of parameter variations for the case studied.

For the entire set of DoE based operating parameter variations test-bed measurements have been carried out for the investigated speed/load points. The measured in-cylinder pressure traces and engine out emission data for NO, soot, CO and unburned hydrocarbons were then used for the assessment of the performance of the combustion/emissions model suite adopted in the CFD calculations.

![Fig. 7: Engine geometry model (left), port/piston bowl configuration (right)](image)

**Table 3: Engine operating conditions and DoE parameter variation range**

<table>
<thead>
<tr>
<th>Load Point</th>
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<tr>
<td>Engine speed</td>
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<tr>
<td>IMEP</td>
<td>8.3 bar</td>
</tr>
<tr>
<td>SOI</td>
<td>1 – 10 deg BTDC</td>
</tr>
<tr>
<td>EGR</td>
<td>12 – 20 %</td>
</tr>
<tr>
<td>Swirl</td>
<td>0 – 74 %</td>
</tr>
<tr>
<td>Inj. Pressure</td>
<td>1200 – 1600 bar</td>
</tr>
</tbody>
</table>

### 3.2 Computational details

In order to enable the large number of 3D CFD calculations of the DoE matrix to be performed within reasonable time, the calculations were done on an
engine segment mesh covering 1/8 of the cylinder/piston bowl arrangement around one single fuel spray assuming cyclic symmetry using AVL FIRE code. Fig. 8 shows a snapshot of the mesh topology at 40 degree crank-angle BTDC position adopting a spray aligned mesh block in order to exclude undesired numerical influences on the spray/combustion results. The mesh size varies over the cycle between 68.000 (BDC) and 24.000 (TDC).

The engine segment calculations for each DoE matrix point were started at the time of inlet valve closure (115 degree crank-angle BTDC) and commenced until opening of the exhaust valves (138 degree crank-angle ATDC).

The crank angle increment during compression phase has been chosen with 1 deg CA. During the injection and combustion phase the increment has been reduced to 0.1 deg CA in order to accurately resolve the fast chemical and physical processes.

The gas side initial conditions at the time of inlet valve closure, i.e. in-cylinder pressure, temperature and residual gas mass fraction, as well as the wall temperature boundary conditions were taken from 1D cycle simulations adopting the AVL BOOST code.

Fig. 8: Set-up of the engine segment model and the CFD calculation within the FIRE Engine Simulation Environment Diesel (ESE Diesel)
A solid body rotation of the in-cylinder flow field at the time of inlet-valve closure was prescribed, with the swirl levels and turbulence intensities extracted from preceding calculations of the entire intake stroke adopting a full 3D computational model.

The fuel side boundary conditions, i.e. hydraulic injection timing and injection rates for the different injection pressure levels were obtained on the basis of 1D hydraulic simulations adopting the AVL HYDSIM code. Parameterization of the hydraulic model was conducted on the basis of selected 3D nozzle flow simulations.

Figure 9 shows the comparison of predicted and measured soot emission indices for different operating conditions within the load point defined in Table 3. Excellent agreement between calculations and experimental measurements is worth mentioning.

**Acknowledgements**

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**References**